442/Phs. 22-23/32411

B.Sc. Semester-III Examination, 2022-23 PHYSICS [Honours]

Course ID: 32411 Course Code: SH/PHS/301/C-5

Course Title: Mathematical Physics-II

Time: 1 Hour 15 Minutes Full Marks: 25

The figures in the right-hand margin indicate marks.

Candidates are required to give their answers in their own words as far as practicable.

UNIT-I

1. Answer any **five** of the following questions:

$$1 \times 5 = 5$$

- a) What is variance?
- b) Define Hermitian matrices.
- c) State Cauchy's theorem.
- d) What is generalized momenta?
- e) Define unitary matrices.
- f) Discuss the nature of singularity of the function

$$f(z) = \frac{1 - \cosh z}{z^2} \text{ at } z = 0.$$

- g) Define similarity transformation.
- h) What do you mean by a symmetric and a skew-symmetric matrix?

UNIT-II

2. Answer any **two** of the following questions:

$$5 \times 2 = 10$$

- a) Is the limit $\lim_{z\to 0} \frac{\operatorname{Re}(z^2) + \operatorname{Im}(z^2)}{z^2}$ exists? 5
- b) There are on average 20 buses per hour at a point but at random times. What is the probability that there are no buses in five minutes?
- c) i) Prove that $\frac{(1+\sqrt{3}i)^{10}}{(1-\sqrt{3}i)^{10}} = -\frac{1}{2} + \frac{\sqrt{3}}{2}i$.
 - ii) Find the roots of $(-1+i)^{\frac{1}{3}}$. 2+3
- d) Evaluate the integral $I = \oint \frac{\sin z}{2z \pi} dz$ over the circle |z|=2.

UNIT-III

3. Answer any **one** of the following question:

$$10 \times 1 = 10$$

a) i) A particle of mass *m* moves in one dimension such that it has the Lagrangian

$$L = \frac{m^2 \dot{x}^4}{12} + m \dot{x}^2 V(x) - V^2(x).$$

ii) Find the eigen values and the corresponding eigen vectors for the

matrix
$$A = \begin{bmatrix} 2 & -2 & 3 \\ 1 & 1 & 1 \\ 1 & 3 & -1 \end{bmatrix}$$
. 4+6

b) Find the residue of $f(z) = \frac{z}{(z^2 + 1)^2}$ at z = i. Find

$$I = \int_0^{2\pi} \frac{d\theta}{5 + 4\cos\theta}$$
 using residue theorem. 3+7
